

2022.10.31 Group meeting

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**Probing the $Z = 6$ spin-orbit
shell gap with $(p,2p)$ quasi-free
scattering reactions**

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Three questions

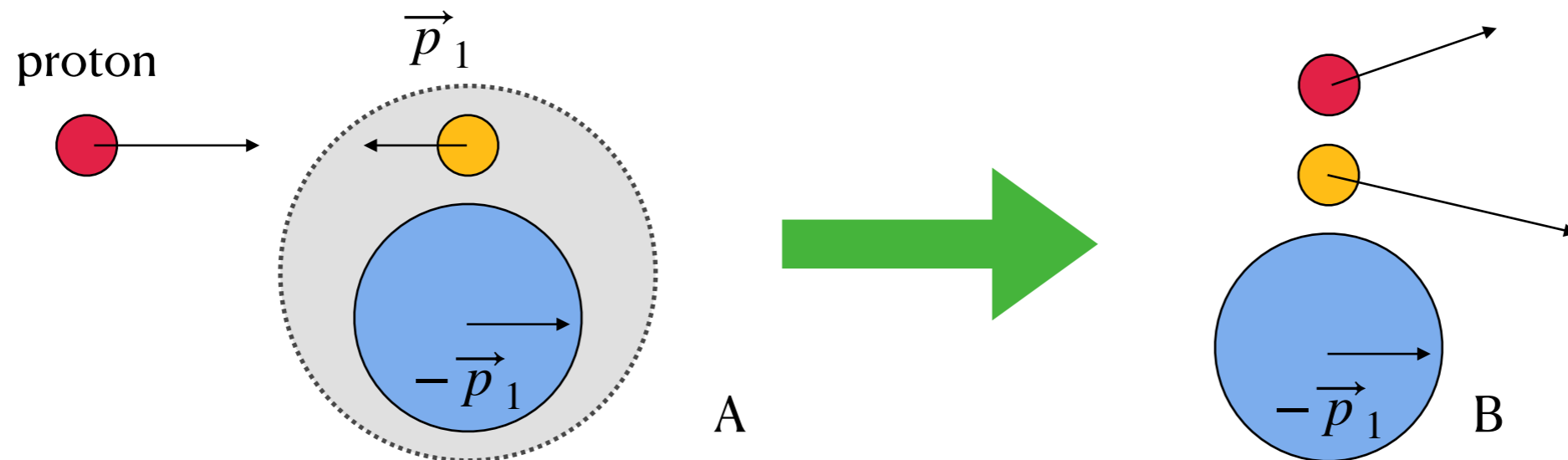
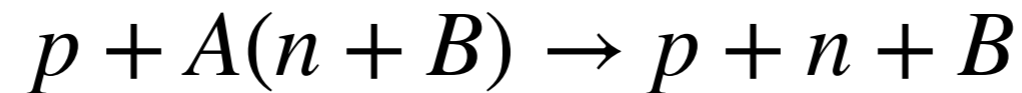
Basic picture of QFS ?

Theoretical framework of QFS ?

**How can the experiment reveal
the reduction of the shell gap?**

Quasi-free scattering

Used to describe (p, pn) reactions



The projectile only interacts only with the removed nucleon, leaving the state of B unchanged.

Calculation

T matrix:

$$T_{p,pN} = \sqrt{S(lj)} \left\langle \chi_{\mathbf{k}'_p}^{(-)} \chi_{\mathbf{k}_N}^{(-)} \left| \tau_{pN} \right| \chi_{\mathbf{k}_p}^{(+)} \psi_{jlm} \right\rangle$$

Fourier transform
of the interaction

$$T_{p,pN} = \sqrt{S(lj)} \int d^3\mathbf{r}'_{pB} d^3\mathbf{r}'_{NB} d^3\mathbf{r}_{pA} d^3\mathbf{r}_{NB}$$

$$\times \tau \left(\mathbf{r}'_{pB}, \mathbf{r}'_{NB}; \mathbf{r}_{pA}, \mathbf{r}_{NB} \right)$$

$$\times \chi_{\mathbf{k}'_p}^{(-)*} \left(\mathbf{r}'_{pB} \right) \chi_{\mathbf{k}_N}^{(-)*} \left(\mathbf{r}'_{NB} \right)$$

$$\times \chi_{\mathbf{k}_p}^{(+)} \left(\mathbf{r}_{pA} \right) \psi_{jlm} \left(\mathbf{r}_{NB} \right)$$

$$\mathbf{r}_{pA} = \mathbf{r}_{pN} + \mathbf{r}_{NB}$$

“the range of the pN interaction is
much smaller than the nuclear size”



Zero-range approximation ?

$$T_{p,pN} = \sqrt{S(lj)} \tau \left(\mathbf{k}'_{pN}, \mathbf{k}_{pN}; E \right) \int d^3\mathbf{r}_{NB}$$

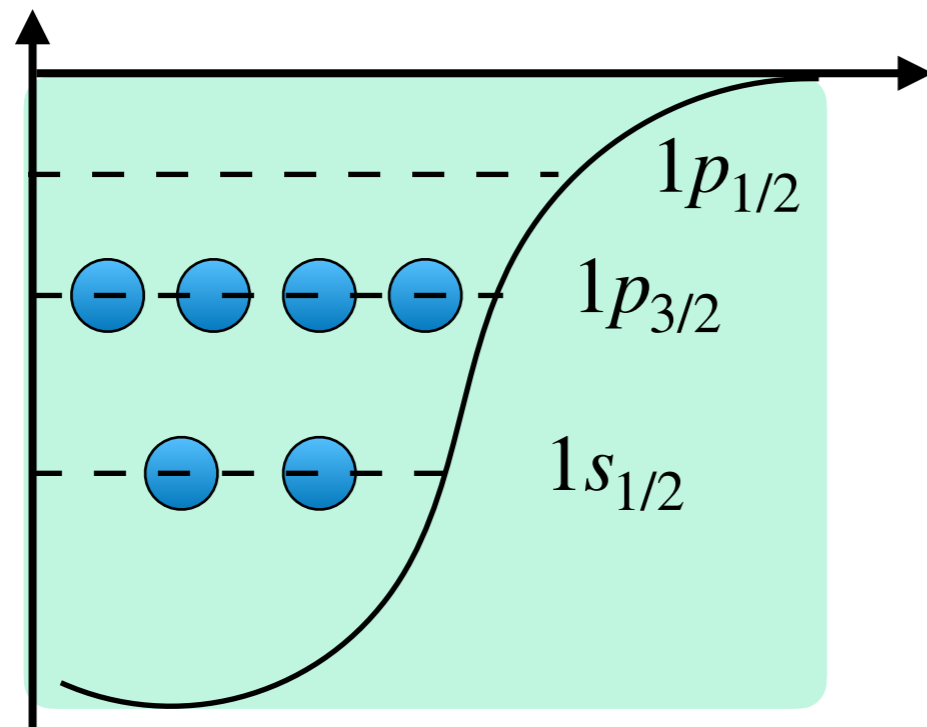
$$\times \chi_{\mathbf{k}'_p}^{(-)*} \left(\mathbf{r}_{NB} \right) \chi_{\mathbf{k}_N}^{(-)*} \left(\mathbf{r}_{NB} \right)$$

$$\times \chi_{\mathbf{k}_p}^{(+)} \left(\alpha \mathbf{r}_{NB} \right) \psi_{jlm} \left(\mathbf{r}_{NB} \right)$$

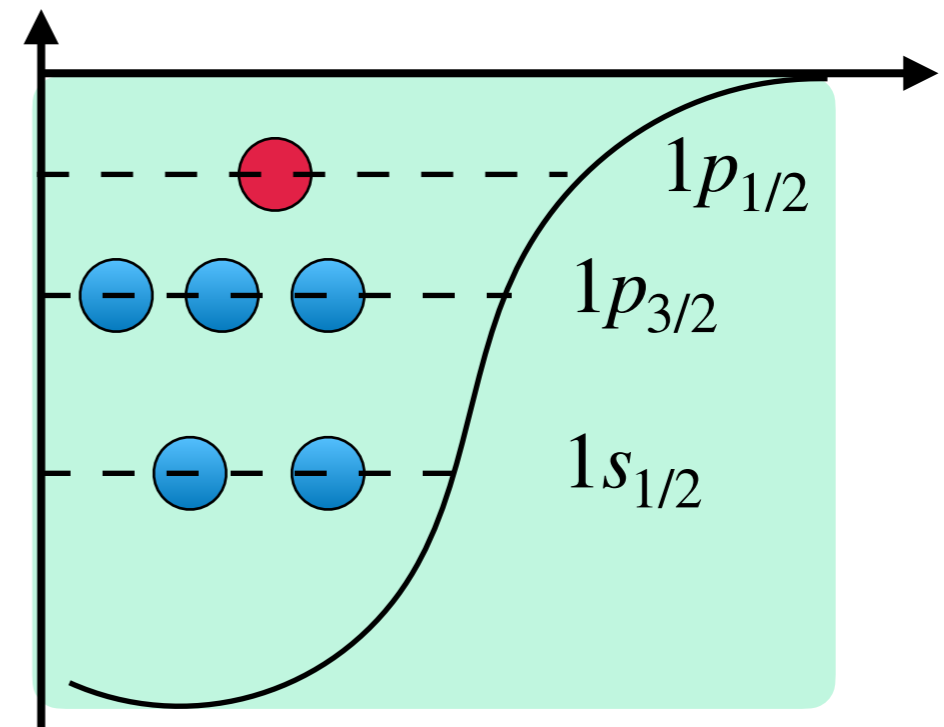
Eikonal approximation:

$$\chi_i(\mathbf{r})^{\text{in(out)}} = \exp \left[i\mathbf{k}_i^{\text{in(out)}} \cdot \mathbf{r} \right] \times \exp \left[-\frac{i}{\hbar v} \int_{a_{\text{in(out)}}}^{b_{\text{in(out)}}} dz' U_i^{\text{in(out)}}(\mathbf{r}') \right]$$

A simple shell model picture



Ground state of O



Proton excitation of O

$$0_1^+ \text{ State of O: } |0_1^+, A-1 \text{ C}\rangle \approx |\nu(sd)^n; J=0\rangle \otimes |\pi(1p_{3/2})^4; J=0\rangle$$

$$2_1^+ \text{ State of O: } |2_1^+, A-1 \text{ C}\rangle \approx \alpha |\nu(sd)^n; J=2\rangle \otimes |\pi(1p_{3/2})^4; J=0\rangle$$

$$+\beta |\nu(sd)^n; J=0\rangle \otimes |\pi(1p_{3/2})^3(1p_{1/2})^1; J=2\rangle$$

Ground state of ${}^A\text{N}$:

$$|1/2^-, {}^A\text{N}\rangle \approx |\nu(sd)^n; J=0\rangle \otimes |\pi(1p_{3/2})^4(1p_{1/2})^1; J=1/2\rangle$$

Some results

	State	Orbital	$\sigma_{\text{exp}}[\text{mb}]$	$\sigma_{\text{theo}}[\text{mb}]$	$C^2 S_{\text{exp}}$
$^{17}\text{N}(p,2p)^{16}\text{C}$	inclusive		3.82(19)		
	0^+	$1p_{1/2}$	2.83(20)	6.171	0.46(3)
	2^+	$1p_{3/2}$	0.68(9)	5.929	0.11(2)
$^{19}\text{N}(p,2p)^{18}\text{C}$	inclusive		3.66(14)		
	0^+	$1p_{1/2}$	2.53(15)	5.267	0.48(3)
	2^+	$1p_{3/2}$	0.45(7)	5.193	0.09(1)
$^{21}\text{N}(p,2p)^{20}\text{C}$	inclusive		2.65(34)		
	0^+	$1p_{1/2}$	1.87(38)	4.554	0.41(8)
	2^+	$1p_{3/2}$	0.78(17)	4.458	0.17(4)

inclusive cross section and
exclusive cross section for a particular single-particle state

How experiment separates cross section induced by different s.p. state?

Data reduction

Reduction of β^2 [2]:

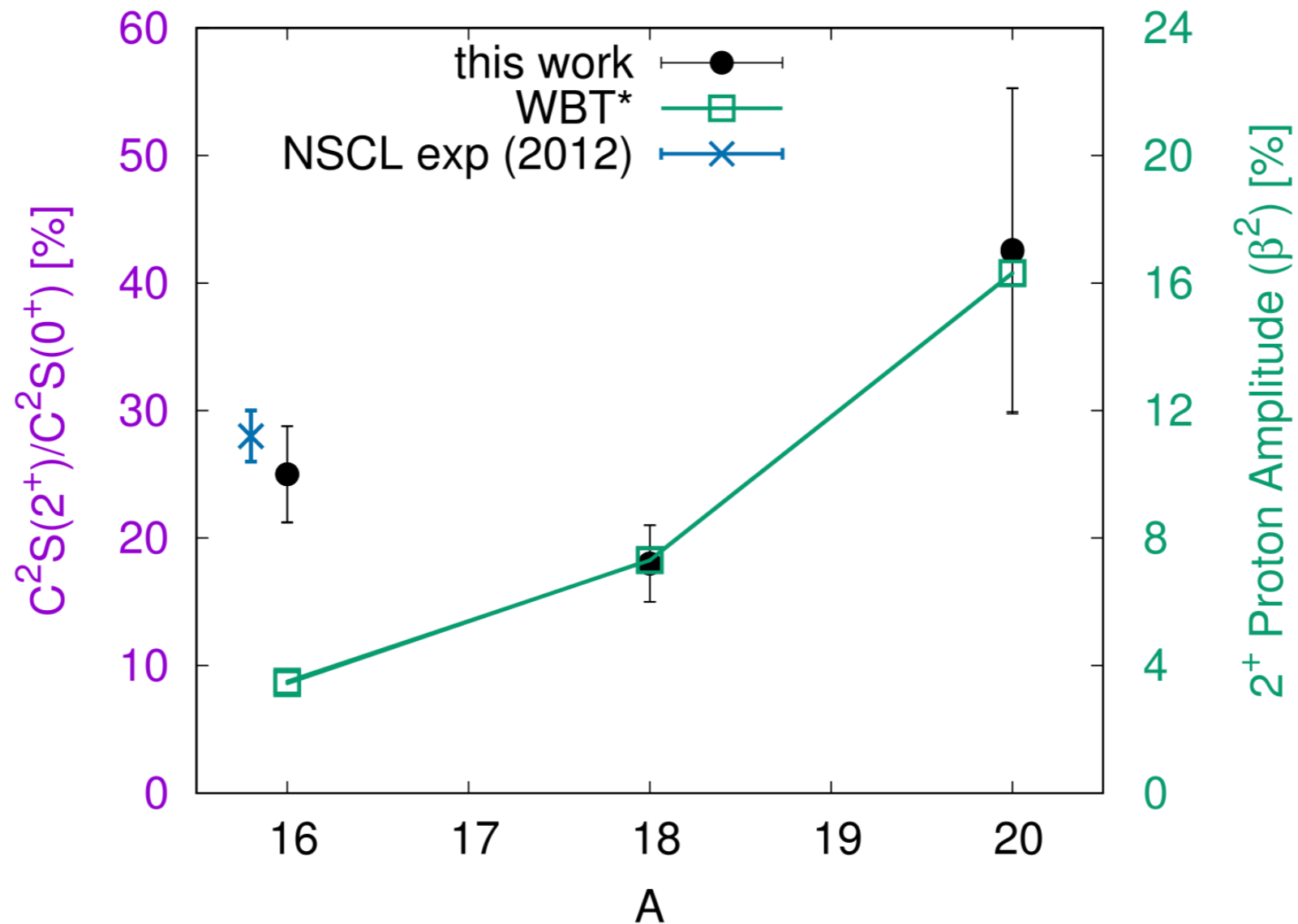
$$\frac{\sigma_{exp}(2_1^+)}{\sigma_{exp}(0_1^+)} \times \frac{\sigma_{theo}(p_{1/2})}{\sigma_{theo}(p_{3/2})} = \frac{C^2S(2_1^+)}{C^2S(0_1^+)} = \beta^2 \times \frac{5}{2}$$

	State	Orbital	σ_{exp} [mb]	σ_{theo} [mb]	C^2S_{exp}	β^2 [%]
$^{17}\text{N}(p,2p)^{16}\text{C}$	inclusive		3.82(19)			
	0^+	$1p_{1/2}$	2.83(20)	6.171	0.46(3)	
	2^+	$1p_{3/2}$	0.68(9)	5.929	0.11(2)	10.0(15)
$^{19}\text{N}(p,2p)^{18}\text{C}$	inclusive		3.66(14)			
	0^+	$1p_{1/2}$	2.53(15)	5.267	0.48(3)	
	2^+	$1p_{3/2}$	0.45(7)	5.193	0.09(1)	7.2(12)
$^{21}\text{N}(p,2p)^{20}\text{C}$	inclusive		2.65(34)			
	0^+	$1p_{1/2}$	1.87(38)	4.554	0.41(8)	
	2^+	$1p_{3/2}$	0.78(17)	4.458	0.17(4)	17.0(51)

Comparison with shell model results

$$\frac{C^2S(2_1^+)}{C^2S(0_1^+)} = \beta^2 \times \frac{5}{2} \quad \text{Scale factor}$$

Ratios
from
experiment



β^2 from
shell
models

A decline is observed in the experiment

Some results

In first order perturbation theory, the proton amplitude is given by:

$$\beta \sim \frac{V_{\pi\nu}}{E_{2_{\pi}^{+}} - E_{2_{\nu}^{+}}} \quad ?$$

$V_{\pi\nu}$: matrix element mixing the unperturbed 2_{π}^{+} and 2_{ν}^{+} states

The denominator is dominated by the difference between the proton $1p_{1/2}$ and $1p_{3/2}$ level energies $\Delta E_{so} = e_{1/2} - e_{3/2}$



“The driving mechanism behind the evolution of the $\pi 1p_{1/2}$ and $\pi 1p_{3/2}$ orbits as function of isospin is the combined effect of the tensor (mainly) and two-body spin-orbit forces acting on the $1p$ protons when neutrons are added in the $d_{5/2}$ and $s_{1/2}$ orbits.”

Summary

1. Carry out QFS experiment of $N(p,2p)C$, get the inclusive and exclusive cross section.
2. Calculate cross sections for different s.p. state based on eikonal approximation.
3. Set up a shell model picture to describe the structure of N and C .
4. Derive the proton amplitude β from ratios of SFs.
5. An increase of β towards the drip line indicates a moderate quenching of $Z = 6$ $1p$ spin-orbit splitting gap.